

Class – X Subject – Mathematics Summative Assessment-I

Time: 3Hours

M.M.80

Section-A

Choose the correct answer and write in your answer sheet

10×1=10

- Q.1 $(1 + 3\sqrt{2})(1 - 3\sqrt{2})$ is
 a. Positive integer b. Negative Integer c. Irrational No. d. None
- Q.2 Sum of an irrational number and a rational number is always:
 a. an irrational b. a rational c. an integer d. a whole number
- Q.3 Which one is not polynomial .
 a. $x^3 - 3x^2 + x + 1$ b. $\sqrt{5}x^2 + x + 1$ c. $8x^{-3} + x + 1$ d. All are polynomial
- Q.4 Value of k for which the system $kx + 2y = 5$, $3x + y = 1$ has unique solution.
 a. $k=6$ b. $k=3$ c. $k \neq 6$ d. both b & c
- Q.5 If $\tan^2 \theta + \frac{1}{\tan^2 \theta} = \sqrt{3}$ then value of $\tan^4 \theta + \frac{1}{\tan^4 \theta}$ is equal to
 a. 3 b. 9 c. 2 d. none
- Q.6 Trigonometric ratio whose value is can not greater than 1
 a. $\tan A$ b. $\cos A$ c. $\sin A$ d. both (b) and (c)
- Q.7 Ratio of areas of two similar triangles whose corresponding sides are 8 cm and 12cm is
 a. $\frac{4}{9}$ b. $\frac{6}{9}$ c. $\frac{2}{3}$ d. $\frac{3}{2}$
- Q.8 QA and PB are perpendiculars to AB .If AQ = 10 PB = 6 and AB=9 then PQ is
 a. 12 b. 5.4 c. 15 d. none
- Q.9 Remainder when $3x^3 + 16x^2 + 21x + 20$ is divided by $x + 4$
 a. 10 b. -10 c. 0 d. none
- Q.10 $\sec^{\theta} (1 - \sin^{\theta}) (\sec^{\theta} + \tan^{\theta})$ equals to
 a. $\sec^2 \theta + \tan^2 \theta$ b. 1 c. -1 d. none

Section-B

Q.11 Consider the number 6^n , Where n is a natural number. Check whether for any value 6^n ends with the digit zero.

Q.12 If α, β are zeroes of quadratic polynomial $kx^2 + 4x + 14$, find the value of k such that

$$(\alpha + \beta)^2 - 2\alpha\beta = 24$$

Q.13 Solve for x and y

$$\frac{x}{a} + \frac{y}{b} = 2, ax - by = a^2 - b^2$$

Q.14 If one diagonal of a trapezium divides the other diagonal in ratio 1:2, Prove that one of the parallel side is double the other.

Q.15 If A, B and C are interior angle of triangle ABC , then show that $\sin\left(\frac{B+C}{2}\right) = \cos\frac{A}{2}$

Q.16 If $7\sin^2\theta + 3\cos^2\theta = 4$, then show that $\tan\theta = \frac{1}{\sqrt{3}}$

Q.17 The following is the distribution of weight (in Kg.) of 40 persons.

Weight(in kg.)	40-45	45-50	50-55	55-60	60-65	65-70	70-75	75-80
No. of persons	4	4	13	5	6	5	2	1

Construct a cumulative frequency distribution of less than type the above data.

Q.18 The weight of tea in 70 packets are shown in the following table:

Weight(in kg)	200-201	201-202	202-203	203-204	204-205	205-206
No. of persons	12	26	20	9	2	1

Section-C

Q.19 Find the H.C.F. of 65 and 117 and express it in the form of $65m+117n$.

Q.20 Find the largest number that will divide 398,436 and 542 leaving remainder 7,11,15, respectively.

Q.21 On dividing $x^3 + x^2 + x - 2$ by a polynomial $g(x)$, the quotient and remainder were $x^2 + 2x + 1$ and $2x - 1$ respectively. Find $g(x)$.

Q.22 α, β are the zeros of the quadratic polynomial $x^2 - (k-1)x + 2(2k-1)$. Find the value of k if

$$\alpha + \beta = \frac{1}{2}\alpha\beta$$

Q.23 Prove that area of equilateral triangle described on the side of a square is half the area of equilateral triangle described on its diagonal.

Q.24 Given ΔABC , $\angle A = 90^\circ$, and $AD \perp BC$, Prove that $AD^2 = BD \cdot CD$

Q.25 Evaluate:

$$\frac{\sec^2 \theta - \cot^2 (90 - \theta)}{5(\sin^2 52^\circ + \sin^2 38^\circ)} - \frac{3 \cdot \cot^2 60^\circ \cdot \operatorname{cosec}^2 72^\circ \cdot \cos^2 18^\circ}{\operatorname{cosec}^2 54^\circ - \tan^2 36^\circ}$$

Q.26 Prove that:

$$\frac{\cos^3 \theta + \sin^3 \theta}{\cos \theta + \sin \theta} + \frac{\cos^3 \theta - \sin^3 \theta}{\cos \theta - \sin \theta} = 2.$$

Q.27 The mean of following distribution is 53. Find the value of p.

Class	0-20	20-40	40-60	60-80	80-100
Frequency	12	15	32	p	13

Q.28 Find the median of following distribution:

Class	5-10	10-15	15-20	20-25	25-30	30-35	35-40	40-45
Frequency	5	6	15	10	5	4	2	2

Section-D

Q.29 Draw the graphs of the pair of linear equation $x - y + 2 = 0$; $4x - y - 4 = 0$. Calculate the area of the triangle formed by the lines so drawn and the x -axis.

Q.30 In a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides. Prove the converse of it

Using the above proved theorem, ΔABC is isosceles triangle with $AC=BC$. if $AB^2=2AC^2$. Prove that ABC is a right angled triangle.

Q.31 If α, β are the zeroes of polynomial $2x^2 + 5x = k$ and $\alpha^2 + \beta^2 + \alpha\beta = \frac{21}{4}$, find the value of k .

Q.32 If $x = a \sin \theta$ and $y = b \tan \theta$ then Prove that $\frac{a^2}{x^2} - \frac{b^2}{y^2} = 1$.

OR Show that $\frac{\cot A + \operatorname{cosec} A - 1}{\cot A - \operatorname{cosec} A + 1} = \frac{1 + \cos A}{\sin A}$

Q.33 If $\sin A + \operatorname{cosec} A = 3$, find the value of $\frac{\sin^4 A + 1}{\sin^2 A}$.

Q.34 Draw the cumulative frequency curve of more than and less than type for the following distribution:

Class	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80	80-90	90-100
Frequency	5	3	4	3	3	4	7	9	7	8